## Geometry Test IB Review Questions

1. Triangle ABC is such that AC is 7 cm , angle $\mathrm{A} \hat{B} C$ is $65^{\circ}$ and angle $A \hat{C} B$ is $30^{\circ}$.
(a) Sketch the triangle writing in the side length and angles.
(b) Calculate the length of AB .
(c) Find the area of triangle ABC.


Answers:
(b) $\qquad$
(c) $\qquad$
2. The diagram shows a circle of radius $R$ and centre $O$. A triangle $A O B$ is drawn inside the circle. The vertices of the triangle are at the centre, $O$, and at two points $A$ and $B$ on the circumference. Angle AÔB is 110 degrees.

(a) Given that the area of the circle is $36 \pi \mathrm{~cm}^{2}$, calculate the length of the radius R .
(b) Calculate the length AB .
(c) Write down the side length L of a square which has the same area as the given circle.


Answers:
(a) $\qquad$
(b) $\qquad$
(c) $\qquad$
3. The diagram below shows a field ABCD with a fence BD crossing it. $\mathrm{AB}=15 \mathrm{~m}, \mathrm{AD}=20 \mathrm{~m}$ and angle $\mathrm{BAD}=110^{\circ}$. $\mathrm{BC}=22 \mathrm{~m}$ and angle $\mathrm{BD} \mathrm{C}=30^{\circ}$.

diagram not to scale
(a) Calculate the length of BD.
(b) Calculate the size of angle B $\hat{C} D$.

One student gave the answer to (a) "correct to 1 significant figure" and used this answer to calculate the size of angle BĈD.
(c) Write down the length of BD correct to 1 significant figure.
(d) Find the size of angle $B \hat{C} D$ that the student calculated, giving your answer correct to 1 decimal place.
(e) Hence find the percentage error in his answer for angle $B \hat{C} D$.
4. The figure shows two adjacent triangular fields ABC and ACD where $\mathrm{AD}=30 \mathrm{~m}, \mathrm{CD}=80$ $\mathrm{m}, \mathrm{BC}=50 \mathrm{~m} . \mathrm{A} \hat{\mathrm{D}} \mathrm{C}=60^{\circ}$ and $\mathrm{B} \hat{\mathrm{A}} \mathrm{C}=30^{\circ}$.

(a) Using triangle ACD calculate the length AC.
(b) Calculate the size of AB C .

5. A cylinder is cut from a solid wooden sphere of radius 8 cm as shown in the diagram. The height of the cylinder is $2 h \mathrm{~cm}$.

(a) Find AE (the radius of the cylinder), in terms of $h$.
(b) Show that the volume ( $V$ ) of the cylinder may be written as

$$
V=2 \pi h\left(64-h^{2}\right) \mathrm{cm}^{3} .
$$

(c) (i) Determine, correct to three significant figures, the height of the cylinder with the greatest volume that can be produced in this way.
(ii) Calculate this greatest volume, giving your answer correct to the nearest $\mathrm{cm}^{3}$.
6. Three right pyramids Andal, Batsu and Cartos were discovered in the dense jungle of Marhartmasol. Each pyramid has a square base with centres A, B and C respectively.


Diagram not to scale

A surveying team was lowered from a helicopter to the top of Andal to take measurements of the area. Andal is 40 metres high. The angle of elevation from the top of Andal to the top of Batsu is $3^{\circ}$. The horizontal distance from A, the centre of the base of Andal, to B, the centre of the base of Batsu is 600 metres.
(a) Use the diagram below to find the height of Batsu.

## Diagram not to scale


(b) Cartos is found to be 92 metres high and the angle of elevation from the top of Andal to the top of Cartos is $4^{\circ}$.
(i) Draw a diagram similar to the diagram in part (a) to show the relationship between Andal and Cartos.
(ii) What is the horizontal distance from A to C ?
(c) The diagram below represents measurements relative to the centres of the bases of the pyramids. The surveyors determined the angle at A to be $110^{\circ}$, and the distance AB to be 600 m .

## Diagram not to scale


(i) What is the distance between B and C? Give your answer to the nearest metre.
(ii) What is the size of angle ACB?
(iii) What is the area of the land inside triangle ABC ?

