

PRE-ALGEBRA & ALGEBRA CONCEPTS

Homework:
Pre-algebra:

Percentages: pg521-1D: all & pg522-1E: 6,7,8
Ratios: pg 524-1F:2,3,7

Algebra:

Distributive: pg526-2A:all
Rearranging Formulas: pg526-2B:all
Substituting into a Formula: You already have done that. So this is optional: pg527-2C
Linear Equations: pg 529-2D:all

How did math started? (its building blocks, so of speak)

1. Numbers:

2. Variable: x, y, l, p, q

3. Expression: Simplify, Evaluate

$x, x+2, x^2, x+2, 2^x, 2^{x-10}, \sin 2x$

4. Equations: $x+2=10, x^2=4, 2^x=8, \sin 2x = \frac{1}{2}$

5. Functions $f(x)=x+2, f(x)=x^2+2, f(x)=2^x, f(x)=\sin x$

SIMPLIFYING

bla, bla, bla, bla, bla

Handwritten mathematical examples and a diagram. On the left, a fraction $\frac{2x^2y^3}{y^2x^{-3}}$ is circled in blue. To its right, the word "BLA" is written. Further right, the expression $2x^5y$ is circled in blue. On the far right, a larger blue oval contains the algebraic simplification: $2x - 5 + 2x + 10$ on the top line and $4x + 5$ on the bottom line.

- Order of Operations
- Like Terms (Polynomials)
- Distributive Property
- Exponents (Radical) Rules
Index laws

Order of Operations: WHY?

$$6 - 4 \times 5$$

$$-14$$

$$6 - 4 \times 5$$

$$10$$

We need RULES!
THUS Oder of Operations

Order of operations

• BEDMAS or PEMDAS

1. $()$ or $[]$ } always inner, then out
2. $\text{exp. or } \sqrt{\quad}$ }
3. Multiplication & Division }
4. Addition & Subtraction } Always from left to right

Example:

$$15 - [(50 - 25) \times 8^2 - 4]$$

$$15 - [25 \times 8^2 - 4]$$

$$15 - [25 \times 64 - 4]$$

$$15 - [1600 - 4]$$

$$15 - 1596$$

$$-1581$$

Like Terms (name the different parts of a polynomial)

$$4x^3 - 2x^2 - 3x + 10$$

- ✓ Degree of Polynomial *Linear → 1*
Quadratic → 2
- ✓ Number of Terms
- ✓ Term
- ✓ Variable *x*
- ✓ Coefficient *i.e. 4; -2; -3*
- ✓ Independent term or constant

Like Terms

• You can only add & subtract like terms

• So what are they? variable and its degree

$$2x^3 - 5x + 10x^2 + 25 - 3x^2 + 2x^3 - 1 + 3x + 2 + 4x^2$$

$$6x^3 + 11x^2 - 2x + 26$$

4 COLORS THEREFORE 4 TERMS

Like Terms

$$2xy + 3x - 3xy + 2y + 4xy - 10$$

$$3xy + 3x + 2y + 10$$

SEE 4 COLORS THEREFORE 4 TERMS

Note: Like Term refers to adding and subtracting

- What happens when you are multiplying/dividing?

$$(2x)(-3x)$$
$$-6x^2$$

$$(2x)(-5y)$$
$$-10xy$$

$$(2x)(-5xy)$$
$$-10xy$$

$$(5xy)(4xy)$$
$$20x^2y^2$$

$$(-8x)(-2xy)$$
$$16x^2y$$

$$\frac{-4x}{-2y}$$

$$\frac{2x}{y}$$

Keep the y in the denominator

Distributive Property

$$2(x-6)$$
$$2x-12$$
$$-3(u+10)$$

$$\frac{2}{5}\left(\frac{3}{4}-\frac{6}{3}\right)$$

$$\frac{1}{3}(2x+10)$$

$$5-2(y+1)$$

$$5-2y-2$$

$$10x+(3x+1)$$

$$\textcircled{*} 10x+3x+1$$

$$10x-(3x+1)$$

$$\textcircled{\otimes} 10x-3x-1$$

Solving equations

Don't use "Guess & Check"

- What does it mean?

$$2x + 5 = 15$$

$$2x = 10$$

$$x = 5$$

linear

- 3 possibilities: 1 solution, No solution, Infinite Solutions

Note: I have never seen a "no solution" and "infinite solutions" in Math Studies, but still, it is good to know.

$$\begin{aligned} 2(x+1) &= 2x+5 \\ 2x+2 &= 2x+5 \\ 2x-2x &= 5-2 \\ 0 &= 3 \end{aligned}$$

$$\begin{aligned} 2(x+3) &= 2x+6 \\ 2x+6 &= 2x+6 \\ 2x-2x &= 6-6 \\ 0 &= 0 \end{aligned}$$

Linear Equations

- 1-step, 2-steps.... Use your method to solve equations. However, I recommend to first simplify each side of the "equal"

i.e.

$$2x - 3(x+1) = 10 - 2x + 4$$

$$\begin{aligned} 2x - 3x - 3 &= 14 - 2x \\ -x - 3 &= 14 - 2x \end{aligned}$$

NOW START SOLVING

$$-x + 2x = 14 + 3$$

$$x = 17$$

Linear equations

• Proportions

$$\frac{x}{3} = \frac{1}{2}$$

$$2x = 3$$

$$\boxed{x = \frac{3}{2}}$$

Tricky.... Put the (....)

$$\frac{(x+2)(x-1)}{7 \quad 4}$$

$$4(x+2) = 7(x-1)$$

$$4x+8 = 7x-7$$

Percentages

① What % is 12 of 215?

$$\frac{?}{100} = \frac{12}{215}$$

$$? \times 215 = 12 \times 100$$

$$? = 5.58\%$$

② 2 is ~~what~~ % of ?

what # is 10% of 225? $\frac{10}{100} = \frac{?}{225}$

③ 12 is 10 % of what ? number?

$$\frac{10}{100} = \frac{12}{?}$$

Percentages and “how many”?

- ① Total **If there are 28 boys in Math Studies or 8 %, how many students are in total in Math Studies?**

$$\begin{aligned}\frac{28}{\text{Total}} &= \frac{8}{100} \\ \text{Total} &= \frac{2800}{8} \\ \text{Total} &= 350 \text{ students}\end{aligned}$$

- ② A portion

Ex:

If 4.8% of the 500 high school students are swedish, how many swedish students are there?

$$\begin{aligned}\frac{\text{swedish}}{500} &= \frac{4.8}{100} \\ \text{swedish} &= \frac{4.8 \times 500}{100} \\ \text{Swedish} &= 24\end{aligned}$$

Ratios:

- Where do you see them?

- 1:5 or $\frac{1}{5}$ or $1/5$