Name: $\qquad$

1. Manuel conducts a survey on a random sample of 751 people to see which television programme type they watch most from the following: Drama, Comedy, Film, News. The results are as follows.

|  | Drama | Comedy | Film | News |
| :--- | :---: | :---: | :---: | :---: |
| Males under 25 | 22 | 65 | 90 | 35 |
| Males 25 and over | 36 | 54 | 67 | 17 |
| Females under 25 | 22 | 59 | 82 | 15 |
| Females 25 and over | 64 | 39 | 38 | 46 |

Manuel decides to ignore the ages and to test at the $5 \%$ level of significance whether the most watched programme type is independent of gender.
(a) Draw a table with 2 rows and 4 columns of data so that Manuel can perform a chi-squared test.
(b) State Manuel's null hypothesis and alternative hypothesis.
(c) Find the expected frequency for the number of females who had "Comedy" as their most-watched programme type. Give your answer to the nearest whole number.
(d) Using your graphic display calculator, or otherwise, find the chi-squared statistic for Manuel's data.
(e) (i) State the number of degrees of freedom available for this calculation.
(ii) The critical value for Manuel's test is 7.815 .Using this or the p -value, state his conclusion with a reason.
2. The veterinarian has gathered the following data about the weight of dogs and the weight of their puppies.
Dog Total

Heavy Light

|  | Heavy | 36 | 27 | 63 |
| :---: | :--- | :---: | :---: | :---: |
| Puppy | Light | 22 | 35 | 57 |
|  | Total | 58 | 62 | 120 |

The veterinarian wishes to test the following hypotheses.
$\mathrm{H}_{0}$ : A puppy's weight is independent of its parent's weight.
$\mathrm{H}_{1}$ : A puppy's weight is related to the weight of its parent.
(a) The table below sets out the elements required to calculate the $\chi^{2}$ value for this data.

|  | $f_{\mathrm{o}}$ | $f_{\mathrm{e}}$ | $f_{\mathrm{e}}-f_{\mathrm{o}}$ | $\left(f_{\mathrm{e}}-f_{\mathrm{o}}\right)^{2}$ | $\left(f_{\mathrm{e}}-f_{\mathrm{o}}\right)^{2} / f_{\mathrm{e}}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| heavy/heavy | 36 | 30.45 | -5.55 | 30.8025 | 1.012 |
| heavy/light | 27 | 32.55 | 5.55 | 30.8025 | 0.946 |
| light/heavy | 22 | 27.55 | 5.55 | 30.8025 | 1.118 |
| light/light | 35 | $a$ | $b$ | $c$ | $d$ |

(i) Write down the values of $a, b, c$, and $d$.
(ii) What is the value of $\chi_{\text {calc }}^{2}$ for this data?
(iii) How many degrees of freedom exist for the contingency table?
(b) The critical value of $\chi^{2}$ for the $5 \%$ significance level is 3.84 . Using this or the p-value, say if $\mathrm{H}_{0}$ should be accepted? Explain why.

